Physicals and Chemical Sciences



General Course Information

PHYS411 Advanced Quantum Mechanics 2021

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0.125 EFTS 15 Points First Semester Course

Course Coordinator

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Timetable

Classes: Monday 11:00, Tuesday 16:00, Thursday 12:00 Currently Jack Erksine 121, but please check your MyTimetable!

I will try to run the three slots a week for about 9 weeks, concluding in Mid May or so. Tutorials are not a fixed day, but will vary depending on the material.

There will be Test, probably in the first week of Term 2.

Description

This advanced course in non-relativistic quantum mechanics covers Dirac notation, time evolution, angular momentum, time-dependent perturbation theory, identical particles. This material should be of practical use to students who need to do quantum-mechanical calculations. It also provides background that will be useful in the PHYS416 Quantum Field Theory course.

Assessment

15% Three to Four Homework Assignments

20% Test at start of Term 2.65% Final Examination

Pre-requisites

Material from PHYS311 (Quantum) is assumed. If you did not take PHYS311 you should obtain a copy of Jenni Adam's notes, since in several places I intend to build on that material. Some material from PHYS313 (E&M) section will also be assumed (e.g. Maxwell's equations in differential form). Material from PHYS326 (Classical Mechanics) will be helpful for appreciating the material but not essential. Knowledge of multivariate calculus, differential equations, and linear algebra is, of course, assumed.

Textbooks

Much of the course is based on the text: *Modern Quantum Mechanics*, J.J. Sakurai. The latest version I have is by Sakurai and Jim Napolitano, 3nd ed. Addison-Wesley, 2011, but I understand there is a newer one. I think that it is a very good book and worth owning. However, there are earlier versions of the book which contain most of the material that I will be using, and you may be able to find one of those. I will provide some notes and extra materials, but these will not be anywhere as comprehensive as the PHYS311 notes.

Goal of the Course

The aim of this course is to provide a thorough understanding of non-relativistic quantum mechanics, with an emphasis on Dirac notation, time evolution, angular momentum theory, time-dependent perturbation theory and creation and annihilation operator techniques.

Learning Outcomes

Students will be able to:

- Manipulate expressions using Dirac's notation.
- Calculate the time-evolution of simple quantum systems.
- Perform calculations using angular-momentum techniques, including the Wigner-Eckart theorem.
- Be able to explain the concept of quantum entanglement and how it might be used for quantum information applications.
- Calculate transition rates using time-dependent perturbation theory.
- [Probably not covered this year, but material will be available for those who are interested:

Apply to use second-quantization techniques to simplify calculations involving systems of many fermions and/or bosons.]

Summary

In the following "Sa1" and "Sa3" refer to the first and second editions of Sakurai, *Modern Quantum Mechanics*.

FC: Fundamental Concepts:

Bras, kets, operators; Measurement; Position, momentum, translation. [Sa1 1.1-1.7, Sa3 1.1-1.7] (4 lectures).

DY: Dynamics:

Schrodinger and Heisenberg pictures; Harmonic Oscillator; Potentials. [Sa1 2.1-2.4, 2.6, Sa3 2.1-2.4, 2.7]. (4 lectures).

AM: Angular Momentum and Quantum Information:

Rotations, commutation relations; Eigenvalues and eigenstates; Addition of angular momenta; Bell's theorem, and entanglement; Quantum Information.

Wigner-Eckart theorem.

[Sa1 3.1-3.3, 3.5-3.7, 3.9-3.10, Sa3 3.1-3.6, 3.8, 3.10-3.11, extra material] (6 lectures).

TDPT Time-dependent perturbation theory.

[Sa1 5.1-5.7, Sa3 5.1-5.5, 5.7-5.8] (4 lectures).

[IP Identical particles: Bosons and Fermions; Second quantization.

[Sa1 6.1–6.4, Sa3 7.1-7.5, extra material].]

General Physics Information

Please consult the document General Information for Physics Students, available on Learn.